Power Series



Question

Which of the following calculations of the term-by-term derivatives of the power series $\sum_{n=1}^{\infty} n^2 x^n$ is valid?

A.
$$\frac{d}{dx} \left(\sum_{n=1}^{\infty} n^2 x^n \right) = \sum_{n=1}^{\infty} 2nx^n$$

$$B. \frac{d}{dx} \left(\sum_{n=1}^{\infty} n^2 x^n \right) = \sum_{n=1}^{\infty} n^3 x^{n-1}$$

C.
$$\frac{d}{dx} \left(\sum_{n=1}^{\infty} n^2 x^n \right) = \sum_{n=1}^{\infty} (2nx^n + n^2(nx^{n-1}))$$

D.
$$\frac{d}{dx} \left(\sum_{n=1}^{\infty} n^2 x^n \right) = \sum_{n=1}^{\infty} (2n)(nx^{n-1})$$