## Power Series

## Question

Which of the following calculations of the term-by-term derivatives of the power series $\sum_{n=1}^{\infty} n^{2} x^{n}$ is valid?

$$
\begin{aligned}
& \text { A. } \frac{d}{d x}\left(\sum_{n=1}^{\infty} n^{2} x^{n}\right)=\sum_{n=1}^{\infty} 2 n x^{n} \\
& \text { B. } \frac{d}{d x}\left(\sum_{n=1}^{\infty} n^{2} x^{n}\right)=\sum_{n=1}^{\infty} n^{3} x^{n-1} \\
& \text { C. } \frac{d}{d x}\left(\sum_{n=1}^{\infty} n^{2} x^{n}\right)=\sum_{n=1}^{\infty}\left(2 n x^{n}+n^{2}\left(n x^{n-1}\right)\right) \\
& \text { D. } \frac{d}{d x}\left(\sum_{n=1}^{\infty} n^{2} x^{n}\right)=\sum_{n=1}^{\infty}(2 n)\left(n x^{n-1}\right)
\end{aligned}
$$

